

Investigating Polynomials (pp. 1 of 3)

Vocabulary

Polynomial – _____

A polynomial can be classified according to how many "terms" it has.

| Category | Sample | Definition |
|----------|---------------------------|----------------------|
| | $\frac{5}{2}x^2y^3$ | One term |
| | $4x^2 - 9x$ | _____ terms |
| | $2x^2 + 3x + 1$ | _____ terms |
| | $3a^4b + 7bc^2 + 6cd - 8$ | _____ or _____ terms |

Degree of a Polynomial – _____

| Sample | Degree of each term | Degree of Polynomial |
|---------------------------|---------------------|----------------------|
| $\frac{5}{2}x^2y^3$ | 5 | 5 |
| $4x^2 - 9x$ | | |
| $2x^2 + 3x + 1$ | | |
| $3a^4b + 7bc^2 + 6cd - 8$ | | |

Operations To simplify polynomials with addition, subtraction, and multiplication:

- Clear grouping symbols using properties of algebra (distributive)
- Combine like terms using properties of algebra (commutative, associative).

Sample Problems

1) $(-4x^2 - 3xy + 5y^2) + 2(3x^2 - 3xy - 5y^2)$ 2) $(3x^2 + 6xy - 7y^2) - (-x^2 + 5xy - 2y^2)$

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Perform the indicated polynomial operations. Simplify answers, and classify each answer by its degree and number of terms.

3) $3xy^2(5x^2y - 6xy^3)$

4) $(x + 8)(x - 3)$

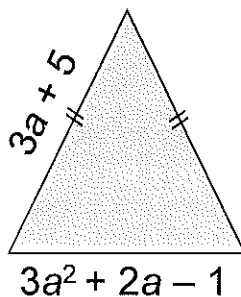
5) $(x + 4)^2$

6) $(2x + 3)(2x - 3)$

Applications:

- 7) A rectangle has a width represented by $4x + 5$ and a length represented by $3x + 2$. What expression can be used to represent the area of the rectangle?

- 8) The diagram below shows an isosceles triangle. Find the expression that represents the perimeter of the triangle.



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Practice Problems

Simplify the following polynomials.

1. $2(4x^2 + 3xy - 7y^2) + (2x^2 - 5xy - 3y^2)$

2. $(5m^2 - 2mp - 6p^2) - 2(-3m^2 + 5mp - p^2)$

3. $2x(x + 5) - x(3 - x)$

4. $5a^2b(7ab^2 + 3a - 4b)$

5. $(3x - 2y)(-4x + y)$

6. $(2x + 1)^2$

7. $(5x + 4)(5x - 4)$

8. $(2n - 3)(n^2 + 5n - 1)$

9. The height of a triangle is represented by the expression $(x + 2)$. The base is represented by $(2x - 8)$. Find the expression that can be used to represent the area of the triangle.

10. The width and length of a rectangle are given in the diagram below. Find the expression that can be used to represent the area of the rectangle.

