

6-6: Rational Exponents (Practice)

Write each expression in radical form, or write each radical in exponential form.

$$1. 5^{\frac{1}{3}} = \sqrt[3]{5}$$

$$2. m^{\frac{4}{7}} = \sqrt[7]{m^4} \text{ or } (\sqrt[7]{m})^4$$

$$3. (m^3)^{\frac{2}{5}} = (\sqrt[5]{n^3})^2 \text{ or } \sqrt[5]{(n^3)^2} \\ = \sqrt[5]{n^6}$$

$$4. \sqrt{79} \quad 79^{1/2}$$

$$5. \sqrt[3]{27m^6n^4} = (27m^6n^4)^{1/3}$$

$$6. \sqrt[5]{2a^{10}b} = (2a^{10}b)^{1/5}$$

Evaluate each expression.

$$7. 81^{\frac{1}{4}} = \sqrt[4]{81} = \boxed{3}$$

$$8. 1024^{\frac{1}{5}} = \sqrt[5]{1024} = \boxed{4}$$

$$9. (-64)^{\frac{2}{3}} = (\sqrt[3]{-64})^2 = (-4)^2 \\ = \boxed{16}$$

$$10. 27^{\frac{1}{3}} \cdot 27^{\frac{4}{3}} = 27^{1/3+4/3} = 27^{5/3}$$

$$= \boxed{27 \sqrt[3]{27^2} \text{ or } 27 \sqrt[3]{729}}$$

$$11. \left(\frac{125}{216}\right)^{\frac{2}{3}} = \left(\sqrt[3]{\frac{125}{216}}\right)^2 = \left(\frac{5}{6}\right)^2 \\ = \boxed{\frac{25}{36}}$$

$$12. \frac{64^{\frac{2}{3}}}{343^{\frac{2}{3}}} = \left(\sqrt[3]{\frac{64}{343}}\right)^2 \\ = \left(\frac{4}{7}\right)^2 = \boxed{\frac{16}{49}}$$

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Simplify each expression.

13. $g^{\frac{4}{7}} \cdot g^{\frac{3}{7}}$

$$g^{\frac{4}{7} + \frac{3}{7}} = g^{\frac{7}{7}} = \boxed{g}$$

14. $s^{\frac{3}{4}} \cdot s^{\frac{13}{4}}$

$$= s^{\frac{3}{4} + \frac{13}{4}} = s^{\frac{16}{4}} \\ = \boxed{s^4}$$

15. $\left(u^{\frac{1}{3}}\right)^{\frac{4}{5}}$

$$u^{\frac{1}{3} \cdot \frac{4}{5}} = \boxed{u^{\frac{4}{15}}}$$

16. $y^{\frac{1}{2}}$

$$\frac{1}{y^{\frac{1}{2}}} = \frac{1}{\sqrt{y}} = \frac{1}{\sqrt{y}} \cdot \frac{\sqrt{y}}{\sqrt{y}} \\ = \boxed{\frac{\sqrt{y}}{y}}$$

17. $b^{\frac{3}{5}}$

already simplified

18. $\frac{q^{\frac{3}{5}}}{q^{\frac{2}{5}}}$

$$q^{3/5 - 2/5} \\ = \boxed{q^{1/5}}$$

19. $\frac{t^{\frac{2}{3}}}{5t^{\frac{1}{2}} \cdot t^{\frac{3}{4}}}$

$$\frac{t^{\frac{2}{3}}}{5t^{\frac{1}{2} + \frac{3}{4}}} = \frac{t^{\frac{2}{3}}}{5t^{-\frac{1}{4}}} \\ = \frac{t^{\frac{2}{3}} \cdot t^{\frac{1}{4}}}{5} = \frac{t^{\frac{8}{12} + \frac{3}{12}}}{5} = \boxed{\frac{t^{\frac{11}{12}}}{5}}$$

20. $\sqrt[10]{8^5}$

$$= 8^{5/10} = 8^{1/2} \text{ or } \sqrt{8} \\ = \sqrt{4 \cdot 2} = \boxed{2\sqrt{2}}$$

21. $\sqrt[4]{6} \cdot 3\sqrt[4]{6}$

$$6^{1/4} \cdot 3(6^{1/4}) = 3(6^{1/4 + 1/4}) \\ = 3(6^{1/2}) \text{ or } \boxed{3\sqrt{6}}$$

22. $\frac{a}{\sqrt{3b}} \cdot \frac{\sqrt{3b}}{\sqrt{3b}}$

$$= \boxed{\frac{a\sqrt{3b}}{3b}}$$

23. **BUSINESS** A company that produces DVDs uses

the formula $C = 88n^{\frac{1}{3}} + 330$ to calculate the cost C in dollars of producing n DVDs per day. What is the company's cost to produce 150 DVDs per day? Round your answer to the nearest dollar.

$$n = 150$$

$$C = 88(150)^{\frac{1}{3}}$$

$$C = 467.57$$

$$\boxed{C = 468}$$